

3.7 Products, Sums, Linear Combinations, and Applications

3. Using the difference-to-product formulas:

$$\begin{aligned} \frac{\cos 3a - \cos 5a}{\sin 3a - \sin 5a} &= -\tan 4a \\ \frac{-2 \sin\left(\frac{3a+5a}{2}\right) \sin\left(\frac{3a-5a}{2}\right)}{2 \sin\left(\frac{3a-5a}{2}\right) \cos\left(\frac{3a+5a}{2}\right)} & \\ &= \frac{\sin 4a}{\cos 4a} \\ &= \tan 4a \end{aligned}$$

4. Using the product-to-sum formula:

$$\begin{aligned} \sin 6\theta \sin 4\theta & \\ \frac{1}{2}(\cos(6\theta - 4\theta) - \cos(6\theta + 4\theta)) & \\ \frac{1}{2}(\cos 2\theta - \cos 10\theta) & \end{aligned}$$